# MAPPING OUT THE QUARK STRUCTURE OF HADRONS IN QCD 

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#### Abstract

In the context of QCD sum rules with nonlocal condensates we present a pion distribution amplitude, which is double-humped with its end-points $x \rightarrow(0,1)$ and strongly suppressed, and show that it matches the CLEO experimental data on the pion-photon transition at the $1 \sigma$ level accuracy, being also in compliance with the CELLO data. We also include some comments on the nucleon distribution amplitude and the nucleon evolution equation.

В подходе правил сумм КХД с нелокальными конденсатами получена пионная амплитуда распределения, являющаяся одновременно двугорбой и сильно подавленной в концевых точках $x \rightarrow(0,1)$. Показано, что она хорошо согласуется с экспериментальными данными по переходному пион-фотонному формфактору как группы CLEO (на уровне 1 стандартного отклонения), так и группы CELLO (более ранними и менее точными). Представлены также некоторые замечания по нуклонной амплитуде распределения и уравнениям эволюции для нее.


## 1. A TRIBUTE TO PROF. EFREMOV'S CELEBRATION OF HIS 70th BIRTHDAY

Prof. Efremov gives us the opportunity to point out in this Festschrift the influence of his work on our own research activities.
A. V.Efremov is one of the inventors of factorization theorems in quantum field theory that are particularly indispensable in applying perturbative QCD in inclusive [1] and exclusive reactions [2,3] involving hadrons. Without these tools, the experimental verification of QCD would constitute an intractable task. Together with his then student A. V. Radyushkin he accomplished the factorization theorems for the meson form factors, linking diagrammatic technique with the operator product expansion (OPE). The grounds for these works were supplied by previous investigations by Efremov [4] and Efremov and collaborators [5].

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Moreover, Efremov and Radyushkin have diagonalized the anomalous dimensions matrix for meson operators (in leading order) in terms of Gegenbauer polynomials and first obtained the asymptotic distribution amplitude (DA) $\varphi\left(x, \mu^{2} \rightarrow \infty\right) \rightarrow \varphi^{\text {as }}(x)=6 x(1-x)[3,6]$.

Factorization theorems [3,6,7] make it possible to calculate various hard processes in QCD involving mesons, in which the meson DAs enter as the central nonperturbative input.

In the context of the present occasion, we are primarily interested in presenting recent achievements in describing the pion characteristics by mapping out its internal quark structure. A short note on the nucleon is also included.

## 2. NONLOCAL CONDENSATES AND PION DISTRIBUTION AMPLITUDE

The pion DA of twist- $2, \varphi_{\pi}\left(x, \mu^{2}\right)$, is a gauge- and process-independent characteristic of the pion that universally specifies the longitudinal momentum $x P$ distribution of valence quarks in the pion with momentum $P$

$$
\begin{equation*}
\left.\langle 0| \bar{d}(0) \gamma^{\mu} \gamma_{5} E(0, z) u(z)|\pi(P)\rangle\right|_{z^{2}=0}=i f_{\pi} P^{\mu} \int_{0}^{1} d x \mathrm{e}^{i x(z P)} \varphi_{\pi}\left(x, \mu^{2}\right) \tag{1}
\end{equation*}
$$

and where $E(0, z)=\mathcal{P} \exp \left[-i g_{s} \int_{0}^{z} t^{a} A_{\mu}^{a}(y) d y^{\mu}\right]$ is a phase factor, path-ordered along the straight line connecting the points 0 and $z$ to preserve gauge invariance.
2.1. Average QCD Vacuum Quark Virtuality $\lambda_{q}^{2}$. The pion DA encapsulates the long-distance effects and therefore reflects the nonperturbative features of the QCD vacuum. The latter can be effectively parameterized in terms of nonlocal condensates, as developed in [8-10] by A. Radyushkin and two of us (A.B. and S. M.). This provides a reliable method of constructing hadron DAs that inherently accounts for the fact that quarks and gluons can flow through the QCD vacuum with nonzero momentum $k_{q}$. This means, in particular, that the average virtuality of vacuum quarks, $\left\langle k_{q}^{2}\right\rangle=\lambda_{q}^{2}$ is not zero, like in the local sum-rule approach [11], but can have values in the range [12] $\lambda_{q}^{2}=\left\langle\bar{q}\left(i g \sigma_{\mu \nu} G^{\mu \nu}\right) q\right\rangle /(2\langle\bar{q} q\rangle)=0.35-0.55 \mathrm{GeV}^{2}$. Therefore, the nonlocal condensates in the coordinate representation, say, $\langle\bar{q}(0) E(0, z) q(z)\rangle$, are no longer constants, but depend on the interval $z^{2}$ in Euclidean space and decay with the correlation length $\Lambda \sim 1 / \lambda_{q}$. Lacking an exact knowledge of nonlocal condensates of higher dimensionality, one has de facto to resort to specific Anzätze [13], in order to parameterize the nonlocal condensates. Nevertheless, it is important to stress that we were able to determine in [14] $\lambda_{q}^{2}$ directly from the CLEO data [15] within the range predicted by QCD sum rules [12] and lattice simulations [13], favoring the value $\lambda_{q}^{2} \simeq 0.4 \mathrm{GeV}^{2}$.
2.2. QCD Sum Rules. The distribution amplitudes $\varphi_{\pi\left(A_{1}\right)}\left(x, \mu^{2}\right)$ for the pion and its first resonance can be related to the nonlocal condensates by means of the following sum rule that is based on the correlator of two axial currents

$$
\begin{align*}
& f_{\pi}^{2} \varphi_{\pi}(x)+ f_{A_{1}}^{2} \varphi_{A_{1}}(x) \exp \left\{-\frac{m_{A_{1}}^{2}}{M^{2}}\right\}= \\
&=\int_{0}^{s_{\pi}^{0}} \rho^{\text {pert }}(x ; s) \mathrm{e}^{-s / M^{2}} d s+\frac{\left\langle\alpha_{s} G G\right\rangle}{24 \pi M^{2}} \Phi_{G}\left(x ; M^{2}\right)+ \\
&+\frac{8 \pi \alpha_{s}\langle\bar{q} q\rangle^{2}}{81 M^{4}} \sum_{i=S, V, T_{1}, T_{2}, T_{3}} \Phi_{i}\left(x ; M^{2}\right), \tag{2}
\end{align*}
$$

where the index $i$ runs over scalar, vector, and tensor condensates [16, 17]; $M^{2}$ is the Borel parameter, and $s_{\pi}^{0}$ is the duality interval in the axial channel. Above, the dependence on the nonlocality parameter enters on the RHS in the way exemplified by the numerically important scalar-condensate contribution

$$
\begin{array}{r}
\Phi_{S}\left(x ; M^{2}\right)=\frac{18}{\bar{\Delta} \Delta^{2}}\{\theta(\bar{x}>\Delta>x) \bar{x}[x+(\Delta-x) \ln (\bar{x})]+(\bar{x} \rightarrow x)+ \\
+\theta(1>\Delta) \theta(\Delta>x>\bar{\Delta})[\bar{\Delta}+(\Delta-2 \bar{x} x) \ln (\Delta)]\} \tag{3}
\end{array}
$$

with $\Delta \equiv \lambda_{q}^{2} /\left(2 M^{2}\right), \bar{\Delta} \equiv 1-\Delta$, and $\bar{x} \equiv 1-x$. In the so-called local approach [11], the end-point contributions $(x \rightarrow 0$ or 1$)$ are strongly enhanced by $\delta(x), \delta^{\prime}(x) \ldots$ because they disregard the finiteness of the vacuum correlation length $\Lambda$ by setting in Eq. (3) $\lambda_{q}^{2} \rightarrow 0$ to obtain

$$
\begin{equation*}
\lim _{\Delta \rightarrow 0} \Phi_{S}\left(x ; M^{2}\right)=9[\delta(x)+\delta(1-x)] \tag{4}
\end{equation*}
$$

In contrast, taking into account the nonlocality of the condensates via $\lambda_{q}^{2}$, leads to a strong suppression of these regions. Due to the end-point suppression property, the sum rule (2) allows us to determine the first ten moments $\left\langle\xi^{N}\right\rangle_{\pi} \equiv$ $\int_{0}^{1} \varphi_{\pi}(x)(2 x-1)^{N} d x$ of the pion DA and independently also the inverse moment $\left\langle x^{-1}\right\rangle_{\pi} \equiv \int_{0}^{1} \varphi_{\pi}(x) x^{-1} d x$ quite accurately (see in $[18,19]$ for more details). The intrinsic accuracy of this procedure admits one to obtain the pion DA moments with uncertainties varying in the range of $10 \%$.
2.3. Models for the Pion Distribution Amplitude. Models for the pion DA, in correspondence with the extracted moments, can be constructed in different ways [8, 17]. However, on the grounds explained above, it appears that twoparameter models, the parameters being the first Gegenbauer coefficients $a_{2}$ and $a_{4}$, enable one to fit all the moment constraints for $\left\langle\xi^{N}\right\rangle_{\pi}$, as well as to reproduce the value of $\left\langle x^{-1}\right\rangle_{\pi}$ within the QCD sum-rule error range, resulting into a «bunch»


Fig. 1. Comparison of selected pion DAs denoted by obvious acronyms: $\varphi^{\text {as }}$ (dotted line) $[3,6], \varphi^{\mathrm{PR}}$ (dashed line) [20], $\varphi^{\mathrm{Dor}}$ (dashed-dotted line) [21], and $\varphi^{\mathrm{BMS}}$ (solid line) [16]. Also shown is the whole «bunch» determined via QCD sum rules with nonlocal condensates [16]. All DAs are normalized at the same scale $\mu_{0}^{2} \approx 1 \mathrm{GeV}^{2}$
of DAs displayed in Fig. 1. The optimum sample out of this «bunch», termed BMS model, is described by the following expression

$$
\begin{equation*}
\varphi^{\mathrm{BMS}}(x)=\varphi^{\mathrm{as}}(x)\left[1+a_{2} C_{2}^{3 / 2}(2 x-1)+a_{4} C_{4}^{3 / 2}(2 x-1)\right] \tag{5}
\end{equation*}
$$

with $a_{2}=+0.20, a_{4}=-0.14$ and is emphasized by a solid line in Fig. 1. The shape of this «bunch» is confirmed by a nondiagonal correlator, based on the QCD sum rules considered in [22].

## 3. CLEO DATA ANALYSIS

The CLEO data [15] on $F_{\pi \gamma}$ provide one rigorous constraint on theoretical models for the pion DA in QCD. Indeed, it was first shown in [23] that these data exclude the CZ pion DA because the prediction derived from it overshoots these data by orders of magnitude.

Very recently, we analyzed $[14,19]$ the CLEO data by combining attributes from QCD light-cone sum rules [24,25], NLO Efremov-Radyushkin-BrodskyLepage (ERBL) [2,3,6] evolution [26,27], and detailed estimates of uncertainties owing to higher-twist contributions and NNLO perturbative corrections [28].

The upshot of this analysis is that the CZ pion DA is excluded at the $4 \sigma$ level of accuracy and - perhaps somewhat surprisingly - that also the asymptotic pion


Fig. 2. Analysis of the CLEO data on $F_{\pi \gamma^{*} \gamma}\left(Q^{2}\right)$ in the $\left(a_{2}, a_{4}\right)$ plane in terms of error regions around the best-fit point $(\boldsymbol{\Psi})$ with the following designations: $1 \sigma$ (dashed line); $2 \sigma$ (solid line); $3 \sigma$ (dashed-dotted line). Various theoretical models are also shown for comparison. The designations are as follows: - the asymptotic DA; $\boldsymbol{x}$ - BMS model; $\square-\mathrm{CZ} \mathrm{DA;} \boldsymbol{+}$ - best-fit point; $\star$ - [29]; $\uparrow$ [20]; $\mathbf{\Delta}$ - instanton models [31]; V - transverse lattice result [30]. The slanted rectangle represents the BMS «bunch» of pion DAs dictated by the nonlocal QCD sum rules for the value $\lambda_{q}^{2}=0.4 \mathrm{GeV}^{2}$. All constraints are evaluated at $\mu^{2}=5.76 \mathrm{GeV}^{2}$ after NLO ERBL evolution

DA lies outside the $3 \sigma$ error ellipse in the ( $a_{2}, a_{4}$ ) plane (see Fig. 2), even if one allows the theoretical uncertainties owing to unknown higher-twist contributions to be of the order of $30 \%$ and presumes that the size of NNLO perturbative corrections is also large. On the other hand, the BMS pion DA calculated with a vacuum virtuality $\lambda_{q}^{2} \simeq 0.4 \mathrm{GeV}^{2}$ was found to be inside the $1 \sigma$ error ellipse, while other rival models, based on differing instantons approaches [20,31], or derived with the aid of lattice simulations [30], are located in the vicinity of the border of the $3 \sigma$ contour. It is worth emphasizing that the more precise the instanton-based models become, the further away from the asymptotic pion DA towards the region of the «bunch» they move (we refer to [19] for more details)*. It was pointed out before in [32] that the CLEO data ask for a broader pion DA than the asymptotic one.

In Fig. 3, $a$ we compare our prediction for the scaled pion-photon transition form factor with those from the CZ model (1) and the asymptotic DA (2). One

[^1]

Fig. 3. a) Light-cone sum-rule predictions for $Q^{2} F_{\gamma^{*} \gamma \rightarrow \pi}\left(Q^{2}\right)$ in comparison with the $\operatorname{CELLO}(\leqslant,[33])$ and the $\operatorname{CLEO}(\mathbf{\Delta},[15])$ experimental data evaluated with the twist-4 parameter value $\delta_{\mathrm{Tw}-4}^{2}=0.19 \mathrm{GeV}^{2}[14,19]$. The predictions correspond to selected pion DAs; viz., $\varphi^{\mathrm{CZ}}$ (curve 1) [11], BMS-«bunch» (shaded strip) [16], and $\varphi^{\text {as }}$ (curve 2) [3,6]. b) Our prediction for $Q^{2} F_{\gamma^{*} \gamma \rightarrow \pi}\left(Q^{2}\right)$ corresponding to the «bunch» of pion DAs in Fig. 1 (shaded strip) in comparison with experimental data for twist-4 parameter values varied in the range $\delta_{\text {Tw- } 4}^{2}=0.15-0.23 \mathrm{GeV}^{2}$
observes that the strip obtained from the «bunch» of DAs is in very good agreement with both the CLEO data and also with the CELLO data [33]. Figure 3, $b$ illustrates in the form of a shaded band the region of uncertainty induced by our limited knowledge of higher-twist contributions. One observes that even the low- $Q^{2}$ CELLO data are in reasonable compliance with the theoretical prediction (the shaded strip).

Let us close this section by mentioning that other approaches claim to be able to describe the CLEO data with the asymptotic pion DA [23,34,35], taking into account only the leading-twist contribution and using only perturbative QCD (see for more details [14]).

## 4. OTHER EXCLUSIVE PROCESSES

Factorization theorems can be extended - at least formally - to baryons and their form factors [6]. The primary goal below is to give a brief summary of main results rather than to review the subject and the status of individual exclusive processes or baryon DAs (for a recent review, we refer to [36]). For instance, the situation concerning the nucleon DA is more controversial compared to the meson case. It is undoubtedly true that the asymptotic nucleon DA is unable to describe the nucleon form factors [6]. On the other hand, asymmetric DAs constructed via moments determined by local QCD sum rules following [11], as, for example, in [37-42] (see Fig.4, $a$ for illustration), seem to yield to strongly suppressed results for the magnetic nucleon form factor when transverse


Fig. 4. a) The heterotic nucleon distribution amplitude, proposed in [41]. b) Spectrum of the anomalous dimensions of trilinear twist-3 quark operators up to the order of $M=400$. The solid lines (upper and lower envelopes of the spectrum) represent logarithmic fits up to the maximum considered order 400 , taking into consideration all orders above 10 . The dashed line gives for comparison a previous logarithmic fit [36] which takes into account all orders up to 150
momentum - intrinsic and Sudakov - effects are included [36, 43]. Valuable information on the inner structure of the nucleon was recently provided in [44] in the context of instantons, where it was shown that the shape of the proton DA is far from the asymptotic one.

While the nonperturbative nature of the nucleon is yet not well-understood, its evolution on the basis of the renormalization-group equation can be performed to a high level of accuracy within QCD perturbation theory. Indeed, within the basis of symmetrized Appell polynomials [36,45], the nucleon evolution equation can be solved by employing factorization of the dependence on the longitudinal momentum from that on the external (large) momentum scale $Q^{2}$ up to any desired polynomial order*. The spectrum of the corresponding anomalous dimensions of trilinear quark operators was also determined $[36,45,46]$ and its large-order behavior seems to increase logarithmically, reflecting the enhanced emission of soft gluons that forces the probability for finding bare quarks to decrease (see Fig. 4, b). This spectrum can be reproduced by the logarithmic fit

$$
\begin{equation*}
\gamma_{n}(M)=c+d \ln (M+b) . \tag{6}
\end{equation*}
$$

The upper envelope of the spectrum is best described by the following values

[^2]of the parameters with their errors: $b=1.90989 \pm 0.00676, c=-0.637947 \pm$ 0.000634 , and $d=0.88822 \pm 0.000119$. For the lower envelope, the corresponding values are $b=3.006 \pm 0.483, c=-0.3954 \pm 0.0290$, and $d=0.59691 \pm 0.00545$. The spacing of eigenvalues at very large order is reproduced by the values $b=$ $-0.027 \pm 0.728, c=-0.2460 \pm 0.0248$, and $d=0.291883 \pm 0.00475$. For every order $M$, there are $M+1$ eigenfunctions of the same order with an excess of symmetric (under the permutation $P_{13}$ ) terms (denoted by black dots in Fig. 4) by one for even orders. The total number of eigenfunctions up to order $M$ is $n_{\max }(M)=\frac{1}{2}(M+1)(M+2)$ and the corresponding $(M+1)$ eigenvalues are obtained by diagonalizing the $(M+1) \times(M+1)$ matrix. Up to order 150 , both sectors (corresponding to the permutation parity $S_{n}= \pm 1$ ) of eigenvalues are included. Beyond that order, for reasons of technical convenience, only the antisymmetric (open circles) ones have been taken into account. The multiplet structure of the anomalous dimensions spectrum was found independently later on [47] in the context of a Hamiltonian approach to the one-dimensional XXX Heisenberg spin magnet of noncompact spin $s=-1$.

## 5. CONCLUDING REMARKS

Our discussion of the pion DA in the context of QCD sum rules with nonlocal condensates shows that the vacuum nonlocality parameter can serve to extract valuable information on the underlying nonperturbative dynamics. The doublehumped shape with suppressed end-points of the derived pion DA is in good agreement with the CLEO data with a $1 \sigma$ accuracy and agrees with the CELLO data as well. Progress of the nonlocal sum-rules approach to encompass threequarks states, like the nucleon, appears promising, while the perturbative apparatus for the evolution of such DAs is already well-developed.

In conclusion, let us mention as a personal statement that the major part of our scientific work depends to a great extent on the power of factorization theorems and their usage in QCD in the context of form factors, structure functions, etc. Therefore, we feel particularly attached to Prof. Efremov, given also that he was the Leader of the BLTPh QCD group, where two of us (A.P.B. and S.V.M.) have been working for over a decade, and he was also one of the opponents of one of us (N. G. S.) in defending his Doctor fiziko-matematicheskih nauk degree.

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[^1]:    *The new model relative to [31], proposed in [21], involves more than two Gegenbauer coefficients and can therefore not be displayed in Fig. 2. However, reverting this model to an approximate one by utilizing only two (effective) Gegenbauer coefficients $a_{2}$ and $a_{4}$ shows that it is close to the $3 \sigma$ error ellipse boundary, as said above.

[^2]:    *The eigenfunctions of the nucleon evolution equation are linear combinations of symmetrized Appell polynomials, appropriately orthonormalized [36].

